MATH 323: Cakulus III	
MATERIALS	
· WebAssign (will include textbook) - around \$120	
· Gradescope (for assignment submission) - free	
· Website (includes syllabus, calendar, practice problems	
- SECTION 12.1: Coordinates in 3-space-	
IDEA of Calculus II: Extend Calculus I, II to functions of several variables	
Some Geometry in 3-Space	
$R^2$ $y = (x,y)$ $R^3 = (x,0,7)_4 - \frac{1}{1-1} (x,y)_{\frac{1}{2}}$	
Some Geometry in Soprice $R^2$ $Y \cap (x,y)$ $\Rightarrow x$ $R^3 (x,0,7)^{\frac{2}{3}} - (x,y,7)$ $\Rightarrow y$ $\Rightarrow x$	
I. Coordinate Planes	
· A coordinate plane is a set of points in which a specified coordinate is O.	
Ex#1: The xy-plane (aka the 7.0 plane) in R3 is N = 2P=(x, y, z) & R3: 2=03	
7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	= "in" : = "neh tro
Fx #2= The yz-plane in 1R3 is { P (x,y,z) & R3 : x = 0}	
x=0	
* Try to turn multivariable problems into single variable ones.	
ASIDE: Distances	
$d(P,Q) = \sqrt{(x_1,y_1,z_1)}$ $ z_1-z_0 $	
$P(x_0, y_0, z_0)$ $ x_1 - x_0  = \frac{1}{ x_0 - x_0 ^2} (y_1 - y_0)^{2^{-1}}$	
1x,-xol t 1 y,-yol	

THM ( Distance Formula) = For  $P = (x_0, y_0, z_0)$  and  $Q = (x_1, y_1, z_1)$  in 3-space, the distance between P and Q is  $d(P, Q) = \sqrt{(x_1 - x_0)^2 + (y_1 - y_0)^2 + (z_1 - z_0)^2}$ .

II. Spheres

· Let r>0 and let PER3. The sphere of vodius r centered at Pis S= 2 QER3: d(P,W=r3

If P has coordinates P= (x, yo, Za), then S= {Q+R3: d(P,Q)=1}

= 
$$\{(x_1,y_1, z_1) \in \mathbb{R}^3: \sqrt{(x_1-x_0)^2+(y_1-y_0)^2+(z_1-z_0)^2} = r\}$$



Spheres are "surfaces of a hollow ball" (NOT SOLID)

A solid ball is defined by  $(x_1 - x_0)^2 + (y_1 - y_0)^2 + (z_1 - z_0)^2 \le r^2$ .

NB: "notabene or "note nell"

\* Everything ne have done so far has analogs in higher dimensions as rell.

Ex: RY (4-space) = {(x,y,z,w): x,y, z, w & R3 has distance formula.

- SECTION 12.2 : Vectors -

· A vector in 163 is a directed line segment, where two vectors are equivalent when they are linear shifts.

